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INVITED REVIEW

Antifreeze proteins: computer simulation studies on the mechanism of ice growth inhibition

Hiroki Nada¹ and Yoshinori Furukawa²

Antifreeze proteins (AFPs), which are present in the bodily fluids of organisms inhabiting cold environments, function as inhibitors of ice growth by binding to certain planes of ice crystals. However, the exact mechanism of ice growth inhibition is still poorly understood as it is exceedingly difficult to experimentally analyze the molecular-scale growth kinetics of ice crystals at the planes to which the proteins bind. This review paper focuses on computer simulation studies on the mechanism of ice growth inhibition by AFPs. Recent molecular dynamics simulations of a growing ice—water interface to which protein is bound have indicated that, when the protein is stably bound to the interface, the growth rate of ice surrounding the protein decreases drastically, owing to depression of the ice melting point through the Gibbs—Thomson effect. The observed decrease in growth rate is expected to correspond to ice growth inhibition in real-world systems. In addition to presenting published simulation studies on the mechanism of ice growth inhibition by AFPs, this review also outlines the direction of future simulation studies in this field.

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INTRODUCTION

Various organisms inhabiting cold environments produce a certain type of protein in their bodies during winter. The proteins are known as antifreeze proteins (AFPs) or antifreeze glycoproteins (AFGPs).¹ Thus far, these proteins have been found in various species of fish,^{2–4} insects,^{5–7} bacteria^{8,9} and plants^{10,11} (hereafter, AFPs and AFGPs are collectively referred to as AFPs).

AFPs function as inhibitors of ice growth.¹ Consequently, liquid water does not completely freeze if it contains dissolved AFPs, even at temperatures lower than the melting point T_m of ice. AFPs have received considerable attention with regards to freeze tolerance and freeze avoidance in organisms,¹² food processing,¹³ cryopreservation¹³ and ice slurries.¹⁴

AFPs are of interest with respect to not only ice crystals, but also other types of crystals. For example, elucidating the mechanism whereby AFPs control ice growth might aid the understanding of the control of biomineral crystal growth by organic molecules, ¹⁵ and might also be useful for developing crystal growth technologies such as crystal morphology engineering, as well as for designing novel composite materials. ¹⁶

A number of experimental studies have been performed to investigate AFPs, 1,17-21 and theoretical models of ice growth inhibition by AFPs have also been proposed. 22-25 Most of the existing theoretical models assume that ice growth inhibition is induced by strong, stable binding of AFPs to certain planes of ice

crystals. The models suggest that the stability of AFP binding to these ice crystal planes and the molecular-scale growth kinetics of ice around AFPs at the planes are vital for understanding the actual mechanism of ice growth inhibition.

To date, the ice crystal planes to which AFPs preferably bind have been experimentally determined for AFPs extracted from a few species. ^{26,27} However, the stability of binding to the ice crystal planes remains unclear. Moreover, it is almost impossible to conduct experimental analyses on the molecular-scale growth kinetics of ice around AFPs at the planes. Thus, despite the considerable efforts in this area, our understanding of the mechanism of ice growth inhibition by AFPs is still poor.

Computer simulation based on a stochastic model such as molecular dynamics (MD) or the Monte Carlo method^{28,29} is a powerful tool for analyzing the stability of AFP binding to ice and the molecular-scale growth kinetics of ice. Thus far, several research groups have used computer simulation for investigating the stable binding conformations of AFP at an ice crystal plane.^{30–37} Recently, we also used MD simulation to analyze the molecular-scale growth kinetics at an ice—water interface to which AFP was bound.^{38,39} These computer simulation studies have contributed to the understanding of the molecular-scale mechanism of ice growth inhibition by AFPs. In this review paper, we discuss the recent progress, as well as the future direction, of computer simulation studies on the mechanism of ice growth inhibition by AFPs.

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FUNDAMENTALS OF AFPs

Here, we briefly summarize the fundamentals of AFPs, namely the structure of various AFPs, the concept of thermal hysteresis, ice growth shapes induced by AFPs and theoretical models of ice growth inhibition by AFPs. Details on these topics can be found in other review papers and books.^{1,17–20,40}

Structure of AFPs

AFPs are classified into several types according to the features of their three-dimensional structure (Figure 1). Type-I AFPs have a simple α -helical structure. $^{41-43}$ The most well-known type-I AFP is winter flounder AFP (wfAFP). 41,42 Furthermore, type-II AFPs are cysteinerich disulphide-stabilized globular proteins, 44,45 type-III AFPs are globular proteins 46 and type-IV AFPs are α -helical proteins rich in glutamine and glutamate. 47 In contrast, insect AFPs have a β -helical structure. 48,49 AFGPs are composed of repeating alanine—alanine—threonine (Ala-Ala-Thr) tripeptide units, and each Thr residue in AFGPs bears a disaccharide residue. 50 AFGPs are highly flexible, and their three-dimensional structure while bound to various planes of ice crystals appears to be rather different from that in bulk water. 51

Thermal hysteresis

Figure 2 shows a schematic image of ice growth inhibition by AFPs, together with examples of ice growth shapes induced by AFPs. Normally, once the nucleation of an ice seed occurs in water at a certain temperature T below T_m , the ice seed continues to grow, and

the entire region of water eventually freezes. However, if AFPs are dissolved in the water, the ice seed growth is inhibited, and therefore the water does not freeze completely. Such inhibition occurs at all T above the freezing temperature T_f , which is considerably lower than T_m . In this way, AFPs produce a difference between T_f and T_m , which is denoted as ΔT_{mf} this difference is thermal hysteresis.⁵²

Normally, an ice crystal grown from pure water is shaped a thin circular disk or hexagonal dendrite with flat {0001} basal plane facets.⁵³ However, AFPs dramatically alter the shape of ice crystals through their ability to inhibit ice growth (see Figure 2). This alteration of ice shape reflects the fact that AFPs selectively bind to certain specific planes of a growing ice crystal, and the ice crystal eventually becomes fully covered with such planes. For example, wfAFP binds to $\{20\overline{2}1\}$ pyramidal planes, resulting in the formation of hexagonal bipyramidal ice crystals covered with 12 {2021} pyramidal planes.¹⁷ AFPs from other species of fish also bind to pyramidal planes, where the crystallographic index of the planes depends on the species. In contrast, spruce budworm AFP (sbwAFP) binds to both basal and prismatic planes, resulting in the formation of thick hexagonal plate ice crystals. 48 Furthermore, tenebrio molitor AFP⁴⁹ induces the formation of rounded lemon-shaped ice crystals, which is assumed to reflect the binding of tenebrio molitor AFP to multiple planes of the ice crystals.⁵⁴

 ΔT_{mf} is shown as a function of the AFP concentration c for typical species in Figure 3a, where ΔT_{mf} increases together with c. As ΔT_{mf} for insect AFPs is much larger than that of fish AFPs, insect AFPs are

Market State			Insects
AFP (Type 2)	AFP (Type 3)	AFGP	Hyperactive
Cystein-rich globular	Globular	(Alanine- alanine-	β-helical
Topa.		dissaccharide groups) repeats	MAN O
	Cystein-rich	Cystein-rich Globular	Cystein-rich globular (Alanine- globular alanine- threonine plus dissaccharide

Figure 1 Illustrations of the structure of typical AFPs.

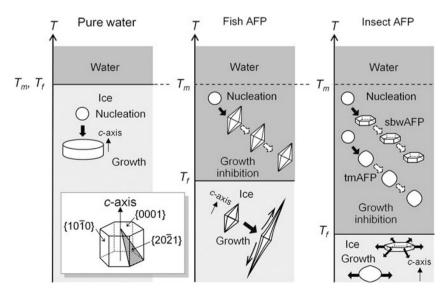


Figure 2 Schematic of the mechanism of ice growth inhibition by AFPs. A full color version of this figure is available at Polymer Journal online.



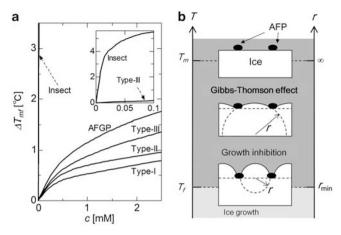


Figure 3 (a) ΔT_{mf} as a function of c for typical species. Plots for ΔT_{mf} for wfAFP, 55,56 sea raven AFP, 45 ocean pout AFP, 57 arctic cod AFGP 50 and sbwAFP 57 are shown as representative examples for type-I, -II, -III and insect AFPs, respectively. For AFGP, data on arctic cod AFGP with molecular mass of 28.8 kDa are shown. (b) Schematic of the Gibbs—Thomson model for ice growth inhibition by AFPs. A full color version of this figure is available at *Polymer Journal* online.

often referred to as hyperactive AFPs.⁵⁴ Note that for all types of AFPs, the decrease in T_m caused by thermodynamic factors, such as changes in the free energy of water by mixing AFPs into it, is negligibly small.

Theoretical model of ice growth inhibition

Thus far, several theoretical models of ice growth inhibition by AFPs have been proposed, $^{22-25}$ the most widely accepted of which is the adsorption–inhibition model. 22 In this model, ice growth inhibition is explained by assuming irreversibly strong binding of AFPs to certain interfaces of ice crystals. 26 In other words, when AFP undergoes irreversibly strong binding to an interface of a growing ice crystal, the interface around the AFP is curved (Figure 3b). Consequently, T_m at the curved interface becomes locally lower than T_m of bulk ice because of the Gibbs–Thomson (or Kelvin) effect. 1

Assuming the growth of a spherical ice crystal with a radius r around AFPs at an interface of an ice crystal, the depression δT_m in T_m caused by the Gibbs–Thomson effect is given as $\delta T_m = 2v\gamma T_m/r\Delta H$, where γ is the free energy of the interface, v is the molar volume and ΔH is the heat of crystallization. δT_m increases as r decreases and reaches a maximum when r decreases to half the distance between two AFP molecules bound to the interface (r_{\min}) ; in this case, the shape of the grown ice crystal corresponds to a hemisphere. It is natural to assume that r_{\min} is inversely proportional to c. Thus, the maximum of δT_m , which corresponds to ΔT_{mf} increases together with c. Consequently, the model based on the Gibbs–Thomson effect qualitatively explains why ice growth is inhibited by the binding of AFP to an ice interface.

However, the estimated δT_m from the model appears to be notably larger than ΔT_{mf} in real-world systems. Shalthough the model assumes irreversibly strong binding of AFPs to interfaces of ice crystals, the binding in real-world systems might not be as strong. AFP binding to interfaces of ice crystals and the molecular-scale growth kinetics of ice around AFPs must be elucidated in order to confirm whether the model applies to real-world systems, and hence these two parameters are crucial to the understanding of the mechanism of ice growth inhibition by AFPs in real-world systems. Unfortunately, analyzing these factors with

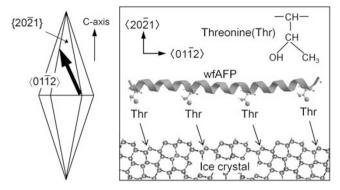


Figure 4 Schematic representing the features of the most energetically stable binding conformation of wfAFP at the ideal pyramidal plane surface. A full color version of this figure is available at *Polymer Journal* online.

existing experimental techniques and equipment is difficult, which leaves computer simulation as a useful tool for analyzing these factors.

COMPUTER SIMULATIONS OF AFP BINDING TO ICE CRYSTALS

A number of computational studies have been performed with the aim to investigate the stability of AFP binding to ice crystals, with particular focus on wfAFP. Wen and Laursen³⁰ investigated the most energetically stable binding conformation of wfAFP at the $\{20\overline{2}1\}$ pyramidal plane by searching for the binding conformation that minimizes the potential energy. They concluded that the most energetically stable binding occurs when wfAFP's α-helical axis aligns with the $\langle 01\bar{1}2 \rangle$ vector, which is in agreement with the binding conformation predicted by Knight et al.26 (Figure 4). Madura et al.³¹ searched for the most energetically stable binding conformation at the pyramidal plane for both the D- and the L-form of wfAFP. Furthermore, Chen and Merz³² used MD simulation to examine the effect of liquid water on the binding conformation of wfAFP at the pyramidal plane. Dalal and Sönnichsen³³ used Monte Carlo simulation to investigate the most energetically stable binding conformation of wfAFP at both the pyramidal plane and the $\{10\overline{1}0\}$ prismatic plane. Jorov et al.34 used Monte Carlo simulation to investigate the effect of hydrophobic interactions between wfAFP and the pyramidal plane on the stability of binding. Similarly, computer simulation has been used to investigate energetically stable binding conformations at ice crystal surfaces for shorthorn sculpin type-I AFP,³⁵ eelpout type-III AFP,^{36,37} sbwAFP38 and tenebrio molitor AFP.59

However, in real-world systems, AFPs bind to ice—water interfaces rather than to planes of ice crystals, and AFPs interact strongly not only with ice, but also with water. Moreover, ice—water interfaces have a diffuse structure. $^{60-63}$ Wierzbicki *et al.* 64 calculated the free energy of wfAFP adsorption at the ice—water interface of the pyramidal plane in equilibrium. This calculation revealed that rather than binding to ice directly, wfAFP is immersed in the interfacial region, where the structure is an intermediate state between ice and water. Wierzbicki *et al.* 33 concluded that binding at the interfacial region becomes most stable when the Thr-Ala-Ala part of wfAFP faces the ice, as opposed to Thr-Ala-Asx in the case of the pyramidal plane.

Consequently, computer simulations for ice crystal planes are not sufficient to elucidate the stability of binding of AFPs to ice in real-world systems. Although several MD simulation studies have focused on AFP binding to an ice–water interface in equilibrium, ^{64–66} simulations should also target a growing ice–water interface, as this is precisely where the ice growth inhibition function of AFPs is manifested in real-world systems.

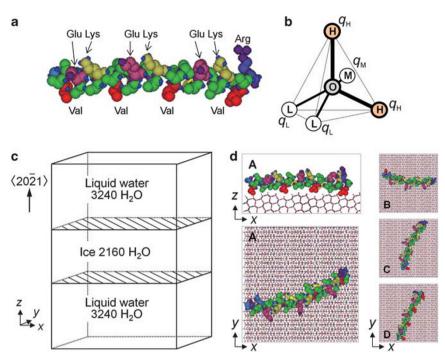


Figure 5 (a) Geometry of water and the positions of interaction sites in the six-site model.⁶⁷ (b) Structure of wfAFP.⁷⁶ (c) A schematic of the simulation system. (d) The initial binding conformations, denoted as A, B, C and D, of AFP at the interface. These initial binding conformations were determined by analyzing the potential energy of the bond between AFP and the ideal pyramidal plane surface. Method used for the analyzing the potential energy can be found in Nada and Furukawa.³⁸

MD SIMULATIONS OF ICE GROWTH INHIBITION BY AFPS

Recently, we performed MD simulations of growing ice–water interfaces by using a wfAFP mutant bound to the pyramidal plane.³⁸ This is the first computer simulation study analyzing the stability of binding of AFP at growing ice–water interfaces and the molecular-scale growth kinetics of ice at the interface. An outline of this study is presented below.

MD simulation

In this study, it was essential to use a water potential model suitable for simulating ice growth. We used a six-site model of rigid water (Figure 5a). 67 Unlike most of the models commonly used for simulation of water, such as SPC/E, 68 TIP4P 69 and TIP5P, 70 the six-site model was proposed for simulation of ice and water near the actual T_m at 1 a.t.m.. For such simulations, several MD studies have demonstrated that the six-site model is suitable for simulating ice growth. $^{63,71-73}$ It naturally follows that the six-site model is also suitable for MD simulation of a growing ice—water interface to which AFP is bound.

In this study, we examined a wfAFP mutant, denoted as VVVV2KE, which was synthesized by Haymet *et al.*⁷⁴ (Figure 5b). In the mutation, the Thr residues of wfAFP are replaced with Val residues, which are strongly hydrophobic (the OH group of each Thr residue is replaced with a CH₃ group). Moreover, two additional Lys-Glu salt bridges are introduced in this mutant. The reason for choosing this mutant was that all of its atomic coordinates have been determined precisely in an experimental study,⁷⁵ which facilitated the construction of a rigid model. This mutant also inhibits the growth of ice by binding to the pyramidal plane,⁷⁶ and the stable binding conformation at the pyramidal plane was the same for both the mutant and the original wfAFP.³⁴ Therefore, it was reasonable to assume that the mechanism of ice growth inhibition associated with

wfAFP was essentially the same as that associated with the mutant (referred to as AFP below). The potential parameters for AFP were determined in accordance with CHARMM by using the param19 file for force field calculations. The LJ parameters for interactions between AFP and water were determined with the Lorentz–Berthelot rules.

The simulation system was a rectangular parallelepiped in which an ice crystal was sandwiched between two liquid water phases (Figure 5c), and thus the system contained two ice–water interfaces at the $\{20\bar{2}1\}$ pyramidal plane. AFP was placed at the surface of each of the two pyramidal interfaces. In this study, four different initial binding conformations of AFP at the interfaces were examined (Figure 5d), where conformation A corresponded to the most energetically stable binding conformation at the ideal pyramidal plane, and conformations B, C and D corresponded to metastable ones. In conformation A, the α -helical axis of AFP was aligned along the $\langle 01\bar{1}2\rangle$ vector, and each Val residue fit inside the groove at the pyramidal plane (see Figure 5d). Notably, conformation B resembled conformation A whereas conformations C and D were vastly different from conformation A.

An MD simulation with a run time covering a period of 4 ns was conducted by maintaining T and pressure at 268 K and 1 atm, respectively. Here, T_m of ice in the system was estimated to be 278 K. Therefore, T=268 K in this simulation corresponded to -10 °C. Details of the simulation method are given in Nada and Furukawa.³⁸

Growth of ice around AFP

Figure 6 shows snapshots of AFP and water molecules in a state resembling ice at 4 ns for all conformations. Water molecules in this state are defined to be connected by hydrogen bonds to each of their four nearest neighbors. The dashed lines show the initial positions of



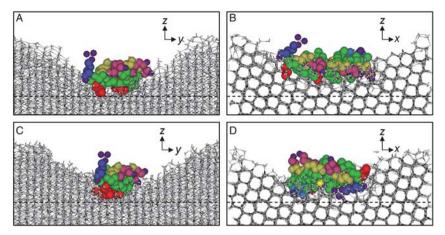


Figure 6 Snapshots of AFP and water molecules forming a structure resembling ice at 4 ns for all conformations. The dashed lines show the initial positions of the interfaces.

the interfaces. Each solid line connecting a pair of water molecules represents a hydrogen bond. It is clear that AFP was partially surrounded by ice that had grown during the simulation. As we describe later, the growth of the surrounding ice had an important role in the stabilization of binding of AFP to the interface.

Figure 7a shows the square displacement Δr_z^2 of the center of mass of AFP as a function of time t in the z direction from the beginning of the simulation, and Figure 7b shows the shift in rotation angle $\Delta \phi$ around the α -helical axis of AFP as a function of t. These two panels in the figure reflect the stability of binding of AFP to the interface for each binding conformation. In other words, initial conformation A was stably bound at its initial position during the growth of ice, whereas initial conformation B became stably bound to the interface only after transforming into conformation A. Initial conformations C and D migrated from their initial positions, indicating unstable binding. Thus, conformation A was deemed to be the most stable at the growing pyramidal interface.

Growth rate of ice

The growth rate R of the ice grown around AFP was estimated for each binding conformation (Figure 8). A large decrease in R occurred during the simulation for conformations A and B, whereas R for conformations C and D was constant over the entire simulation period. Thus, the results indicate that a large decrease in the R occurred only for ice surrounding AFP that was stably bound to the interface, where the observed decrease in R likely corresponded to ice growth inhibition by AFP.

Note that the ice interfaces surrounding AFP for conformations A and B were curved. Therefore, we suspected that the decrease in R observed for conformations A and B originated from a depression in T_m at the curved interfaces owing to the Gibbs–Thomson effect. Therefore, using the parameters associated with the Gibbs–Thomson effect, we estimated δT_m at the curved interface as 5 K by assuming that ice grown around AFP was in the shape of a column with $r=3.45\,\mathrm{nm}$, which was approximately half of the dimension of the system in the y direction. As T of the system was $-10\,^{\circ}\mathrm{C}$, T at the curved interfaces was expected to be $-5\,^{\circ}\mathrm{C}$.

In order to confirm whether this expectation for the value of T at the curved interfaces was correct, the value of R for ice at -5 °C as obtained in the simulation was compared with the value from an experimental study.⁵³ The experimentally obtained value of R at -5 °C was about 2 cm s^{-1} , which is of the same order of magnitude

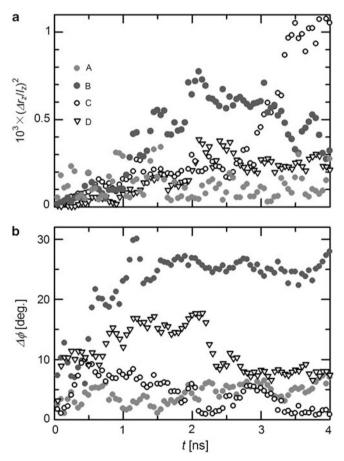


Figure 7 (a) Square displacement Δr_z^2 of the center of mass of AFP in the z direction from the beginning of the simulation as a function of time t, where l_z is the cell length in the z direction. (b) Shifts in the rotation angle $\Delta \phi$ around the α -helical axis of AFP as a function of t. A full color version of this figure is available at *Polymer Journal* online.

as that in the period of 2–4 ns in the simulation (5.9 and 6.3 cm s⁻¹ for conformations A and B, respectively), which confirms that the observed decrease in R for conformations A and B was attributable mainly to a depression in T_m at the curved interfaces due to the Gibbs–Thomson effect. The unchanged value of R for conformations C and D is attributable to the migration of AFP during ice growth; in

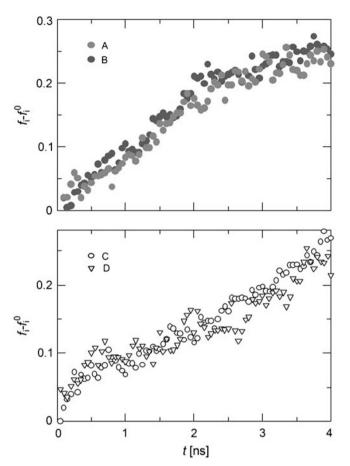


Figure 8 Fraction $f_{\rm ILM}$ of ice-like water molecules in the system as a function of t. Here, $f_{\rm ILM}{}^{\rm O}$ denotes $f_{\rm ILM}$ at the beginning of the simulation. The increase in f_{ILM} together with t reflects the growth of ice, and the slope of the $f_{\rm ILM}$ -t relation corresponds to the growth rate R. Values of R (in cm s⁻¹) as estimated from the slopes of the f_{IIM} -t relations were 19.0 (0-2 ns) and 5.9 (2-4 ns) for conformation A, 16.9 (0-2 ns) and 6.3 (2-4 ns) for conformation B, 10.4 (0-2 ns) and 14.1 (2-4 ns) for conformation C, and 8.7 (0-2 ns) and 12.5 (2-4 ns) for conformation D. A full color version of this figure is available at Polymer Journal online.

other words, the migration hindered the formation of a curved interface, and therefore the depression in T_m at the ice interface because of the Gibbs-Thomson effect was negligibly small.

Stability of AFP binding at growing interface

Next, we discuss the observation that binding conformation A was the most stable at the growing pyramidal interface. In binding conformation A, hydrophobic Val residues bound to ice and hydrophilic residues were exposed to the surrounding liquid water. Notably, binding conformation A was the same as the most stable binding conformation at a pyramidal interface in equilibrium as obtained by Jorov et al.³⁴, who explained the stability of this conformation as follows. The binding of hydrophobic Val residues to ice produces an entropy gain as compared with the case in which those residues are exposed to liquid water because liquid water molecules surrounding each hydrophobic Val residue tend to form a cage-like structure, causing loss of entropy. Moreover, the exposure of hydrophilic residues to liquid water produces an enthalpy gain as the molecules of liquid water rearrange themselves to form hydrogen bonds with the hydrophilic residues. These entropy and enthalpy gains explain why

binding conformation A was the most stable at the pyramidal interfaces in equilibrium.

To determine whether the explanation for the most stable binding conformation at the pyramidal interface in equilibrium is sufficient for explaining the binding conformation at the growing pyramidal interface, we also performed an MD simulation for the pyramidal interface in equilibrium to which AFP was bound in conformation A. However, stable binding of AFP to the pyramidal interface in equilibrium was not observed. This result indicates that the attraction between AFP and the interface was not sufficient to produce a stable binding conformation. Thus, the above explanation is not sufficient for explaining the most stable binding conformation at growing pyramidal interfaces.

At the growing pyramidal interfaces, AFP was partially surrounded by ice that had grown during the simulation. We found that the absolute value of the attractive force between AFP and the growing ice increased significantly after the growth of the surrounding ice, thus stabilizing the binding of AFP to the pyramidal interface. Thus, we concluded that the growth of ice surrounding AFP was necessary in order to promote stable AFP binding to pyramidal interface and subsequent inhibition of ice growth.

MD simulation for prismatic interfaces

Investigating the growth kinetics at other ice planes is also important as the formation of a hexagonal bipyramidal ice crystal in the presence of AFP reflects the anisotropy of ice in terms of R. Thus, in this study, we also performed an MD simulation for a growing icewater interface in the {1010} prismatic plane to which AFP was bound.³⁸ Two initial binding conformations, namely the most energetically stable conformation and a metastable one at the ideal prismatic plane, were examined as the initial binding conformations at the growing prismatic interface.

In either of the binding conformations, AFP did not bind stably to the prismatic interface (Figure 9a), and R did not change substantially during the simulation (Figure 9b). These results might not be sufficient to conclude whether AFP inhibits the growth of ice at the prismatic interface. However, the results are consistent with the fact that AFP inhibits the growth of ice only at the pyramidal plane in real-world systems. Consequently, we believe that the present MD simulation study provides important results that contribute toward the understanding of the mechanism of ice growth inhibition by AFPs in real-world systems.

However, more detailed studies are necessary in order to clarify certain aspects the mechanism of ice growth inhibition by AFPs. For example, the MD simulation described above was carried out under the assumption that the pyramidal plane existed as a facet plane from the beginning. However, the pyramidal plane appears as a result of growth in real-world systems.⁷⁷ Therefore, it is also important to investigate the mechanism of pyramidal plane formation during the growth of ice crystals in the presence of AFPs.

Notably, the above MD simulation for the prismatic interface indicates a change in the binding conformation of AFP.⁷⁸ Specifically, during the growth of ice at the prismatic interface, AFP molecules gradually tilted in such a way that their α-helical axes became parallel to the pyramidal plane (Figure 9c). If the α-helical axes of AFP molecules become stably aligned with the $\langle 01\bar{1}2 \rangle$ vector, a drastic decrease in R might be observed, as in the case of the pyramidal interface. Thus, the observed tilt of the α-helical axis of AFP might correspond to the initial step of the process of pyramidal plane formation, which necessitates further inquiry.



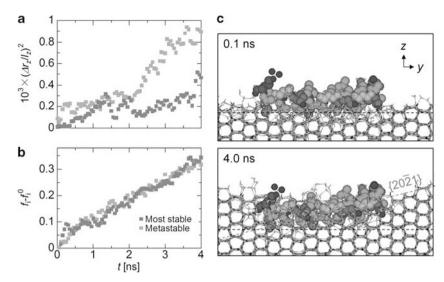


Figure 9 (a) Δr_z^2 for the most stable and a metastable binding conformation of AFP as a function of t for the prismatic interface. (b) f_{ILM} as a function of t for the prismatic interface. (c) Snapshots of the most energetically stable binding conformation of AFP at the ideal prismatic plane and the surrounding structure of water molecules resembling ice at the prismatic interface at 0.1 and 4.0 ns. A full color version of this figure is available at *Polymer Journal* online.

DISCUSSION

Simulation methodology

It is important to establish whether the mechanism of ice growth inhibition proposed on the basis of the MD simulation study using mutant wfAFP also applies to AFPs from other species. Recently, we performed similar MD simulations for a growing ice-water interface of the prismatic plane to which sbwAFP was bound.³⁹ As in the case of mutant wfAFP, a large decrease in R was observed for ice grown around sbwAFP that was stably bound to the interface. This finding supports the hypothesis that the decrease in R was attributable to a decrease in T_m due to the Gibbs-Thomson effect at the curved interface surrounding sbwAFP. More extensive MD simulation studies on AFPs from other species are necessary in order to determine whether the same mechanism of ice growth inhibition is universal. Nevertheless, the abovementioned MD simulation studies using mutant wfAFP and sbwAFP have reliably demonstrated that molecular processes associated with ice growth inhibition can be directly observed with the aid of MD simulations of a growing ice-water interface to which AFP is bound.

For a thorough understanding of the mechanism of ice growth inhibition by AFPs, it is also important to elucidate the mechanism by which ice crystals undergo a morphological change from a sphere or a circular disk into a polygon covered with specific planes where AFPs inhibit ice growth. However, it has been impossible to observe such morphological changes in the simulations conducted so far due to the use of a directional growth system in which ice growth occurred only for a single crystallographic orientation.

Recently, we also carried out an MD simulation of ice growth at a high pressure by introducing a system in which ice crystals were allowed to grow freely in all directions normal to their *c*-axis (free-growth system), and successfully analyzed the formation mechanism of ice crystals with hexagonal plates.⁷³ If a large free-growth system is used for MD simulation of ice growth in the presence of AFPs, morphological changes induced in crystals by AFPs can be directly observed, thus contributing toward a thorough understanding of the mechanism of ice growth inhibition by AFPs in real-world systems.

Direction of future simulation studies

Finally, we discuss the direction of future simulation studies on the mechanism of ice growth inhibition by AFPs. One such direction involves simulation studies on hyperactive AFPs. In this regard, Scotter et al.⁵⁴ have argued that the hyperactivity of certain AFPs stems from their binding to multiple planes of ice crystals, including the basal plane. For example, sbwAFP binds to both prismatic and basal planes of ice. 48 The question naturally arises as to why hyperactive AFPs bind to multiple planes of ice crystals. Garnham et al.⁷⁹ have suggested that water at the surface of ice crystals to which hyperactive AFPs are bound forms a clathrate-like structure, which can adhere to multiple planes of ice. As computer simulation is a powerful tool for analyzing the structure of water around AFPs,80 MD simulation studies should be performed for multiple planes of ice crystals by considering the structure of water at the surface of ice crystals to which hyperactive AFP is bound. For sbwAFP, we have already performed an MD simulation study for the prismatic plane,³⁹ and we intend to extend this study to the basal plane.

Another direction of future work involves the elucidation of the mechanism of ice growth promotion by AFPs. AFPs can promote the growth of ice at planes to which they do not bind. ⁸¹ For example, wfAFP inhibits the growth of ice at pyramidal planes while simultaneously promoting the growth of ice at basal planes, ⁸² which is the reason for the formation of hexagonal bipyramidal ice crystals in the presence of wfAFP. Thus, an investigation of the mechanism of ice growth promotion by AFPs is also necessary for a thorough understanding of the mechanism of ice growth inhibition by AFPs in real-world systems. Computer simulation is also expected to serve as a powerful tool for resolving the mechanism of ice growth promotion.

SUMMARY

In this review, we presented computer simulation studies concerning the mechanism of ice growth inhibition by AFPs. The understanding of this mechanism depends on the elucidation of the stability of AFP binding to various interfaces of ice crystals and the growth kinetics of ice surrounding AFPs at these interfaces. Currently, computer simulation based on intermolecular interaction is the only available tool for analyzing these processes in detail.

A number of computer simulation studies on the mechanism of ice growth inhibition by AFPs have been carried out to date, most of which have focused on the binding of AFPs to various planes of ice crystals or to ice-water interfaces in equilibrium. Recently, an MD simulation study was carried out with respect to growing ice-water interfaces of the pyramidal plane in the presence of AFPs, ³⁸ as a result of which a molecular-scale mechanism of ice growth inhibition by AFPs was proposed. A subsequent MD simulation study involving sbwAFP also suggested essentially the same molecular-scale mechanism of ice growth inhibition.³⁹ Therefore, simulation studies on AFPs from other species are expected to provide an even deeper understanding of the mechanism of ice growth inhibition, and largescale simulations of free growth systems are expected to contribute toward the elucidating the morphological changes induced in ice crystals by AFPs.

In conclusion, the molecular-scale mechanism of ice growth inhibition by AFPs can be directly analyzed with the aid of computer simulation based on intermolecular interaction. More detailed and extensive computer simulation studies should be conducted for a thorough understanding of the mechanism of ice growth inhibition by AFPs in real-world systems. Similarly, computer simulation is also expected to expand our knowledge regarding the mechanism of crystal growth control by impurities, such as the growth control of mineral crystals by organic molecules. 15,16

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